

# Performance Prediction of NUMA Placement A Machine-Learning Approach

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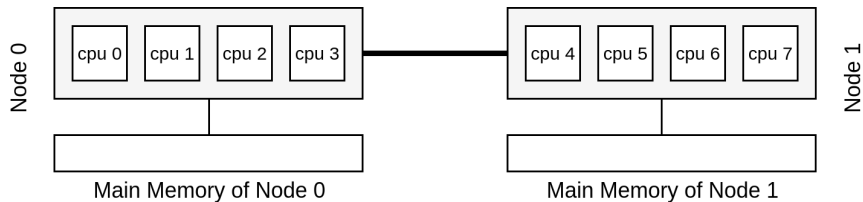
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- Placement of threads and memory matters
  - Common wisdom: Memory locality is the best policy
  - But not always feasible

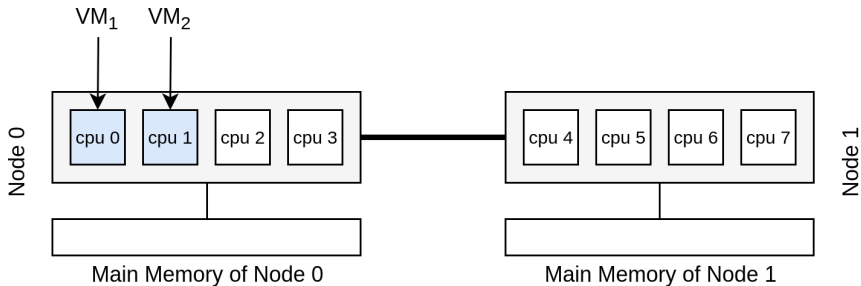
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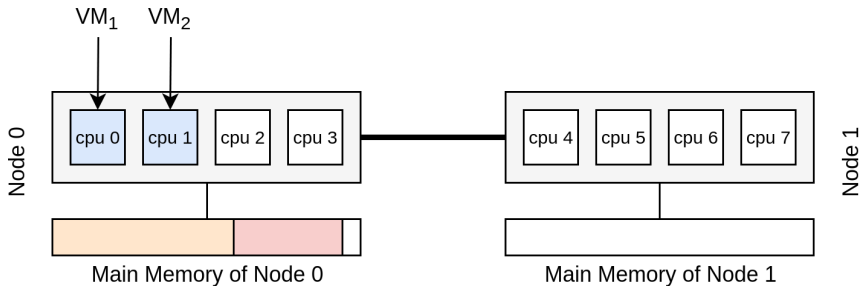




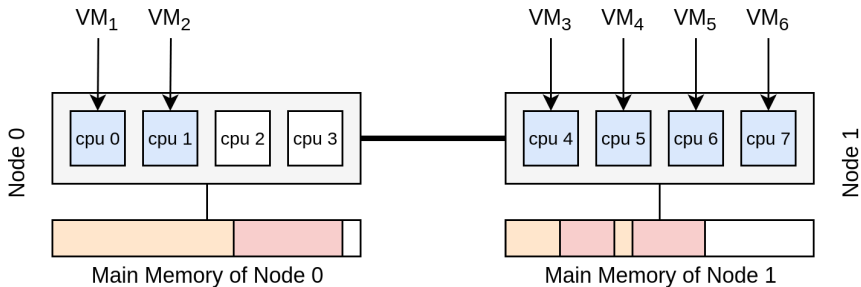
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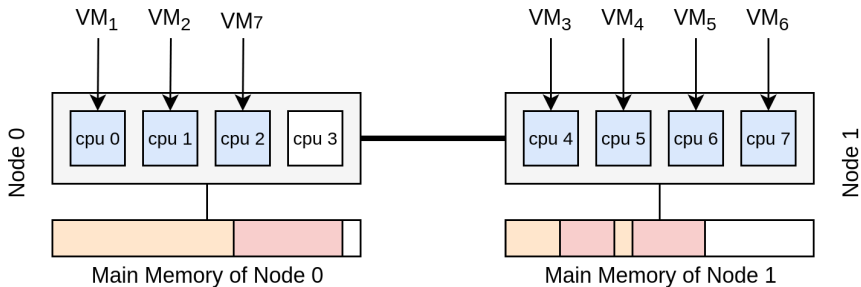
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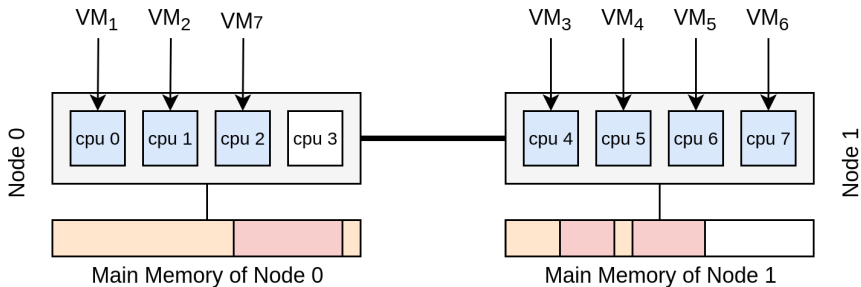
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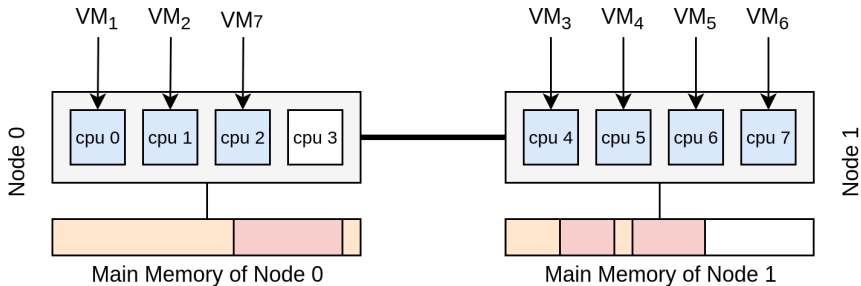
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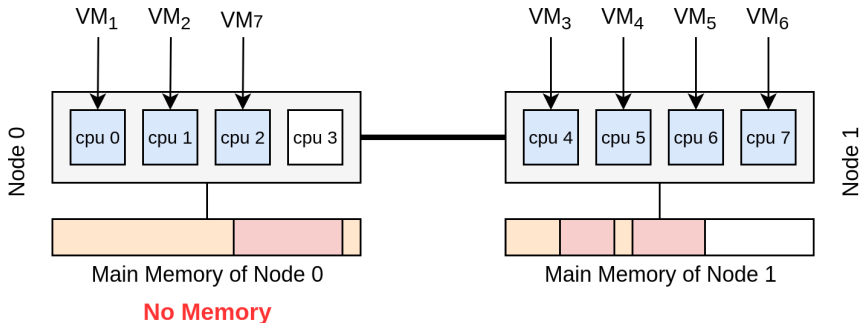


# Problematic Scenario



**No Memory**

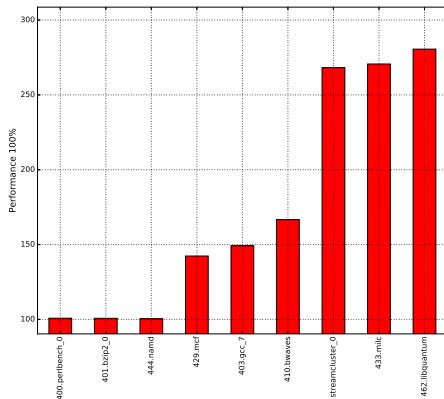
# Problematic Scenario



Which VM to move?

# Motivation

Not all applications are affected in the same way by the placement of core and memory





# In a nutshell

We want to predict the impact on performance of core and memory placement in non-uniform memory access (NUMA) systems

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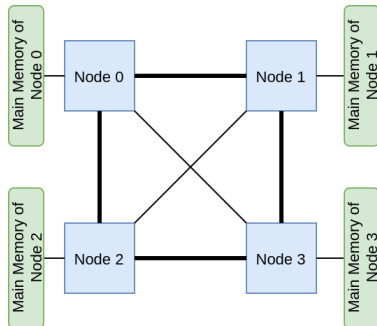
## Our Approach

- Measure parameters from applications
- Model performance using non-linear functions
- Train the functions with machine learning techniques
- Evaluate the predictions

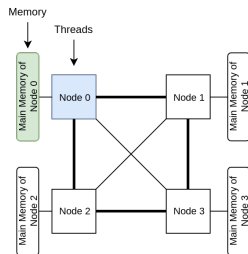
- 1 Platform Details and Benchmarking
- 2 Application parameters and Correlations
- 3 Modeling
- 4 Conclusions and Future work

## Characteristics

- 4 nodes
- Intel Xeon E5-4620, 2.2GHz
- Sandy Bridge
- 8 cores per node (2 threads)
- 64GB RAM per node
- Cache
  - L1 32KB, shared per core
  - L2 256KB, shared per core
  - L3 (LLC) 16MB, shared per NUMA node

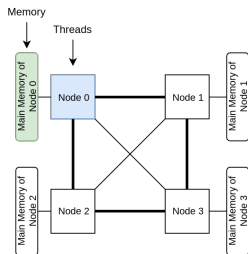


# Placement Scenarios

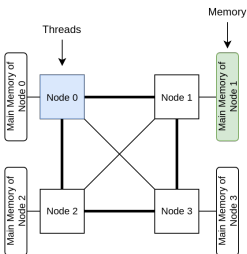


(a) Local

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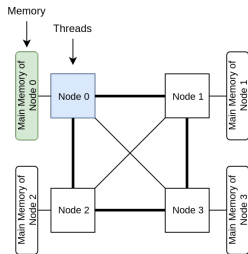


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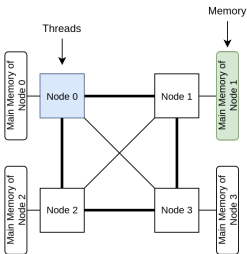


(b) Remote near

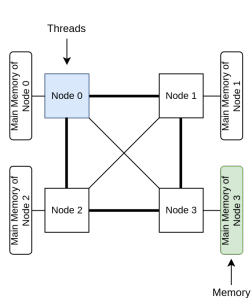
# Placement Scenarios



(a) Local



(b) Remote near



(c) Remote far



## numactl

- Provides necessary information about the system (nodes, processors)
- Allows to perform interleave and membind (remote) executions

## perf

- Measures the parameters of our applications by using the performance counters

- **Spec2006**
- **Parsec**

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  - 26 different benchmarks
  - Multiple input files
  - A total of 52 different executions
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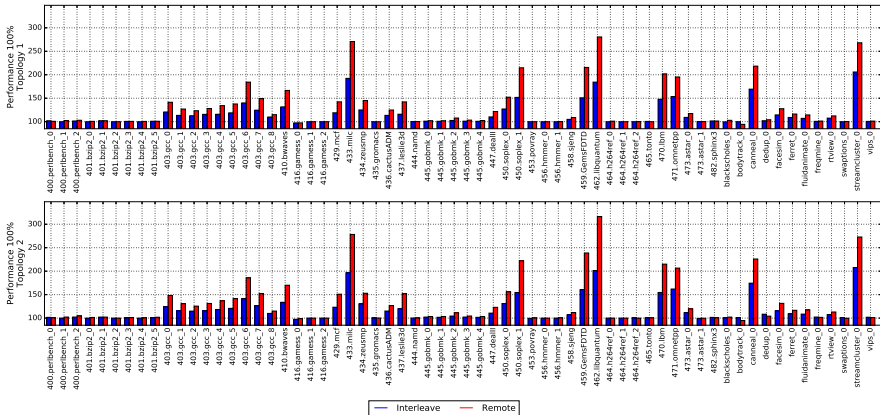
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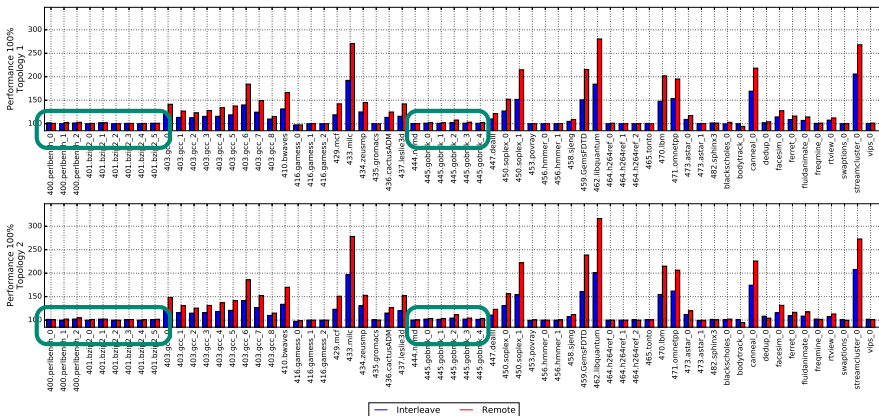
- $\text{Performance}(i,j) = \frac{\text{Total Time}(i,j)}{\text{Total Time}_{local}} \cdot 100\%$

# Performance



## Impact of NUMA placement on performance

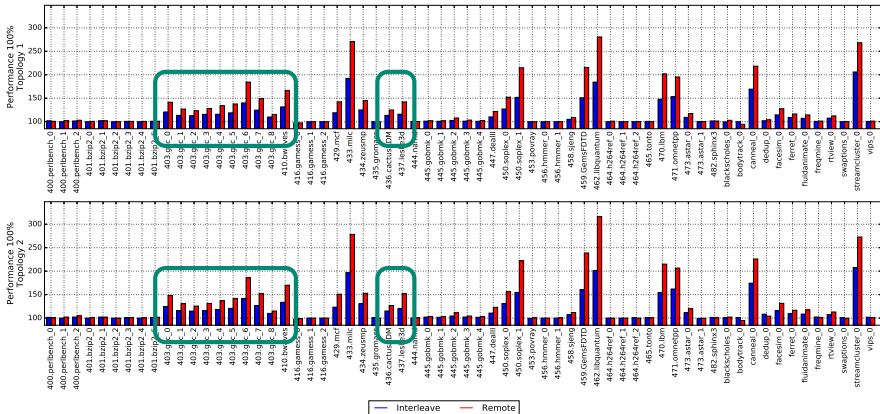
# Performance



## 1. Low impact to performance

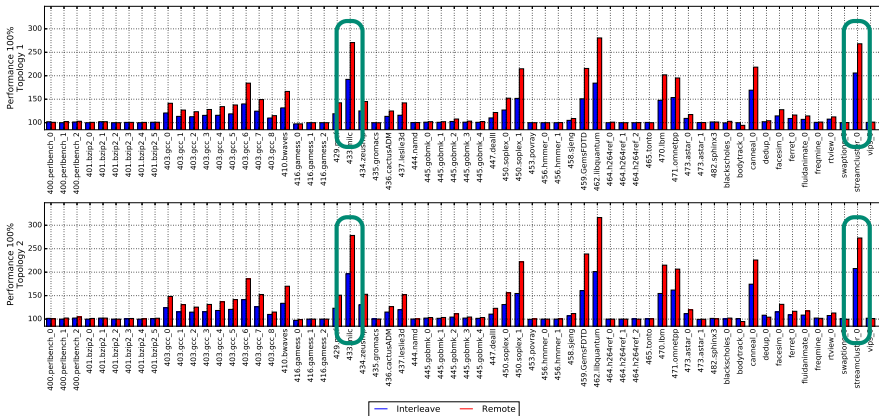


# Performance



## 2. Medium impact to performance

# Performance



## 3. High impact to performance

## 1 Last level Cache Misses per Kilo Instructions

$$\text{MPKI} = \frac{\sum_{i=1}^t \text{LLC-load-misses}[i] + \sum_{i=1}^t \text{LLC-store-misses}[i]}{\sum_{i=1}^t \text{instructions}[i]} \cdot 1000$$

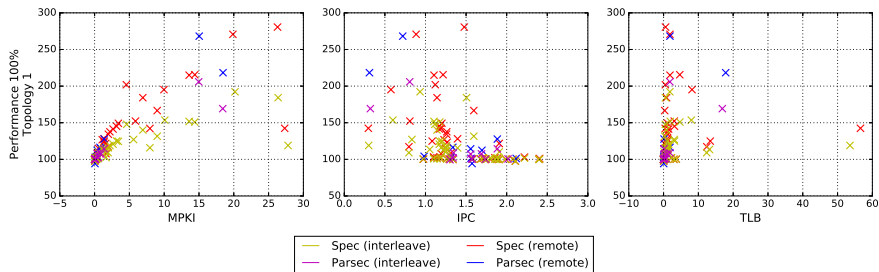
## 2 Instructions per Cycle

$$\text{IPC} = \frac{\sum_{i=1}^t \text{instructions}[i]}{\sum_{i=1}^t \text{cpu-cycles}[i]}$$

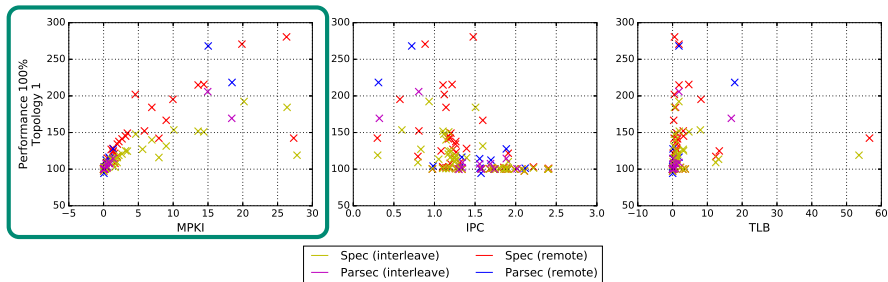
## 3 TLB Misses per Kilo Instructions

$$\text{TLB} = \frac{\sum_{i=1}^t \text{dTLB-load-misses}[i] + \sum_{i=1}^t \text{dTLB-store-misses}[i]}{\sum_{i=1}^t \text{instructions}[i]} \cdot 1000$$

# Correlating Parameters with Performance

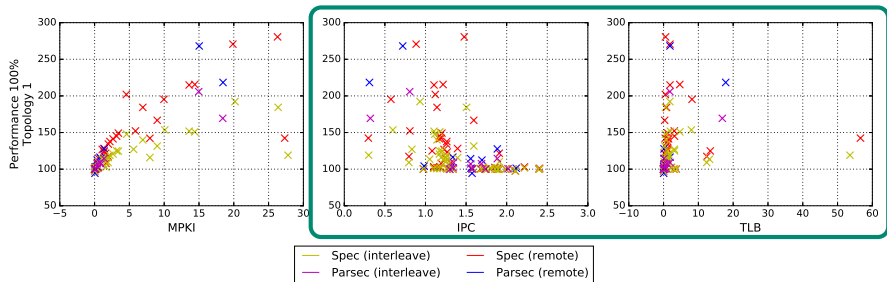


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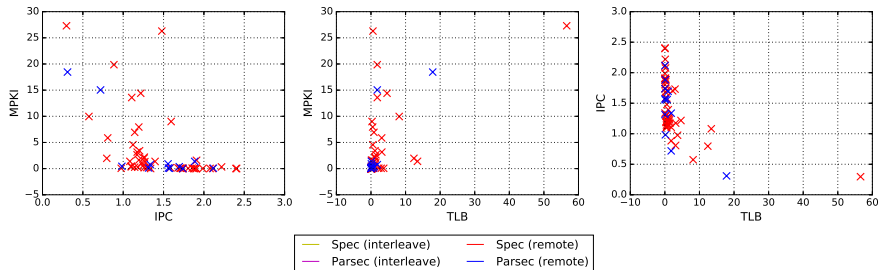
Approach with logarithmic function

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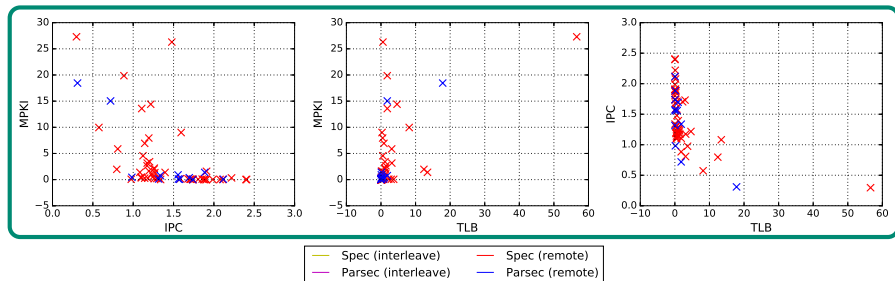


Approach with non-linear function

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Approach with non-linear function



# Generating Candidate Models

The terms are divided into

- 1 Basic
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## Dominant term

- $a_j X_i^{n_1}$
- $a_j \log(X_i + 1)^{n_1}$
- $a_j \log(X_i + 1)^{n_1} + a_{j+1} X_i^{n_2}$

## Secondary term

- $a_j X_i^{n_1}$

Size	Parameters
1	MPKI
	IPC
	TLB
2	MPKI, IPC
	MPKI, TLB
	IPC, TLB
3	MPKI, IPC, TLB

## Correlations

- Rank  
Maximum number of different parameters

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- $a_i \left( \prod_{j=1}^{\text{rank}} X_j^{n_k+j-1} \right)$

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We automatically generate models following a model generation approach similar to “Fast multi-parameter performance modeling” [CLUSTER'16]

# Model Training

To train and evaluate the accuracy of the generated prediction models

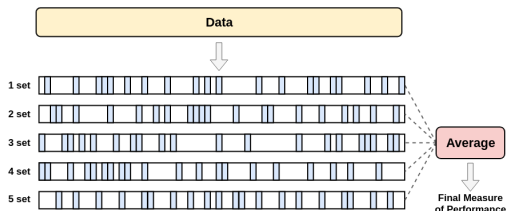


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## Cross Validation

- Random subsampling validation
- Repeated 5 times
- Randomly generated sets (44 train, 20 test)
- Sets may overlap
- Final score: average of all test sets



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Best possible score is 1.0 and it can be negative



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## Metrics

- 1  $R^2$  (coefficient of determination)  
Best possible score is 1.0 and it can be negative
- 2 MAE (mean absolute error)  
Best possible score is 0

Top	Function	$R^2$	MAE
1	$a_1 \cdot \log(x_2 + 1)^{n_1} + a_2 \cdot x_1^{n_2} + a_3 \cdot x_3 + b$	0.9311	5.3154
2	$a_1 \cdot x_1^{n_1} + a_2 \cdot x_2^{n_2} + a_3 \cdot x_3 + b$	0.9303	5.3562
3	$a_1 \cdot \log(x_1 + 1) + a_2 \cdot x_1 + a_3 \cdot x_2^{n_1} + a_4 \cdot x_3 + b$	0.9291	5.4005
4	$a_1 \cdot \log(x_2 + 1) + a_2 \cdot x_1 + a_3 \cdot x_3 + a_4 \cdot (x_2^{n_1} \cdot x_1^{n_2}) + b$	0.9283	5.3818
5	$a_1 \cdot x_1 + a_2 \cdot x_2 + a_3 \cdot x_3 + a_4 \cdot (x_1^{n_1} \cdot x_2^{n_2}) + b$	0.9278	5.4170
6	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_1 + a_3 \cdot x_2^{n_2} + a_4 \cdot x_3 + b$	0.9275	5.4801
7	$a_1 \cdot \log(x_1 + 1) + a_2 \cdot x_1 + a_3 \cdot x_2 + a_4 \cdot x_3 + b$	0.9254	5.6392
8	$a_1 \cdot \log(x_2 + 1)^{n_1} + a_2 \cdot x_2 + a_3 \cdot x_1^{n_2} + a_4 \cdot x_3 + b$	0.9254	5.3471
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11	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_2^{n_2} + a_3 \cdot x_3 + b$	0.9234	5.8351
12	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_2 + a_3 \cdot x_3 + a_4 \cdot (x_1^{n_2} \cdot x_2^{n_3}) + b$	0.9229	5.6140

# Results

Top	Function	$R^2$	MAE
1	$a_1 \cdot \log(x_2 + 1)^{n_1} + a_2 \cdot x_1^{n_2} + a_3 \cdot x_3 + b$	0.9311	5.3154
2	$a_1 \cdot x_1^{n_1} + a_2 \cdot x_2^{n_2} + a_3 \cdot x_3 + b$	0.9303	5.3562
3	$a_1 \cdot \log(x_1 + 1) + a_2 \cdot x_1 + a_3 \cdot x_2^{n_1} + a_4 \cdot x_3 + b$	0.9291	5.4005
4	$a_1 \cdot \log(x_2 + 1) + a_2 \cdot x_1 + a_3 \cdot x_3 + a_4 \cdot (x_2^{n_1} \cdot x_1^{n_2}) + b$	0.9283	5.3818
5	$a_1 \cdot x_1 + a_2 \cdot x_2 + a_3 \cdot x_3 + a_4 \cdot (x_1^{n_1} \cdot x_2^{n_2}) + b$	0.9278	5.4170
6	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_1 + a_3 \cdot x_2^{n_2} + a_4 \cdot x_3 + b$	0.9275	5.4801
7	$a_1 \cdot \log(x_1 + 1) + a_2 \cdot x_1 + a_3 \cdot x_2 + a_4 \cdot x_3 + b$	0.9254	5.6392
8	$a_1 \cdot \log(x_2 + 1)^{n_1} + a_2 \cdot x_2 + a_3 \cdot x_1^{n_2} + a_4 \cdot x_3 + b$	0.9254	5.3471
9	$a_1 \cdot \log(x_1 + 1) + a_2 \cdot x_1^{n_1} + a_3 \cdot x_2 + a_4 \cdot x_3 + b$	0.9246	5.6528
10	$a_1 \cdot \log(x_2 + 1) + a_2 \cdot x_1^{n_1} + a_3 \cdot x_3 + b$	0.9236	5.8177
11	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_2^{n_2} + a_3 \cdot x_3 + b$	0.9234	5.8351
12	$a_1 \cdot \log(x_1 + 1)^{n_1} + a_2 \cdot x_2 + a_3 \cdot x_3 + a_4 \cdot (x_1^{n_2} \cdot x_2^{n_3}) + b$	0.9229	5.6140

Best function:  $R^2 = 0.9311$  and MAE = 5.3154



# Challenges on Training

## Problems

- We need to have at least as many measurement points as are the most volatile variables
- Training time is high due to the free variables  $n_i$
- Many functions will fail in training
- The functions that would fail in training will take a long time

## Solutions

- The free variables  $n_i$  are assigned discrete values within the range  $[-2, -1.5, -1, -0.5, 0.5, 1, 1.5, 2]$
- The maximum number of terms is at most 7
- The correlation powers are the same as the basic terms



## Conclusions

- Studied the performance with respect to NUMA placement
- Correlated the performance with MPKI, IPC, and TLB
- Built models that can predict performance with high accuracy

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## Future work

- Study larger scale NUMA systems
- Model different execution and placement scenarios
- Extend the model with information regarding machine status

# Thank you



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